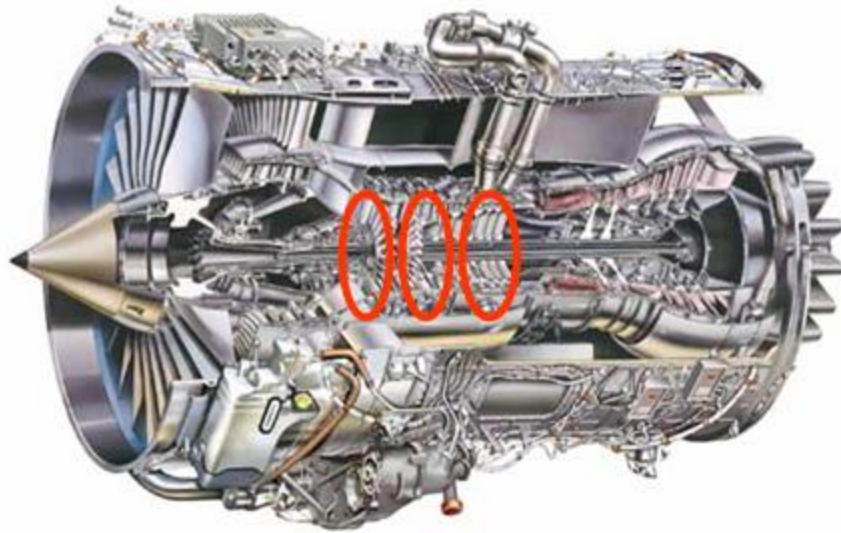
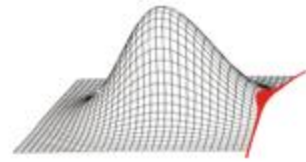


# **Probabilistische CFD-Simulation einer Hochdruckverdichterstufe unter Berücksichtigung von Fertigungstoleranzen**

**Alexander Lange, Matthias Voigt, Konrad Vogeler (TU Dresden)  
Henner Schrapp, Erik Johann, Volker Gümmer (RRD)**

**funded by German Government (LuFo IV) and  
Rolls-Royce Deutschland Ltd & Co KG**

**Dresden, 9. Oktober 2009**



target:

influence of manufacturing tolerances on properties of compressor



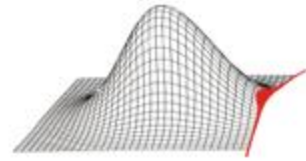
measurement of HPC blades to obtain geometric variations



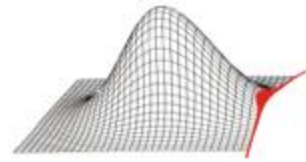
probabilistic  
CFD simulations



compressor characteristics with scatter

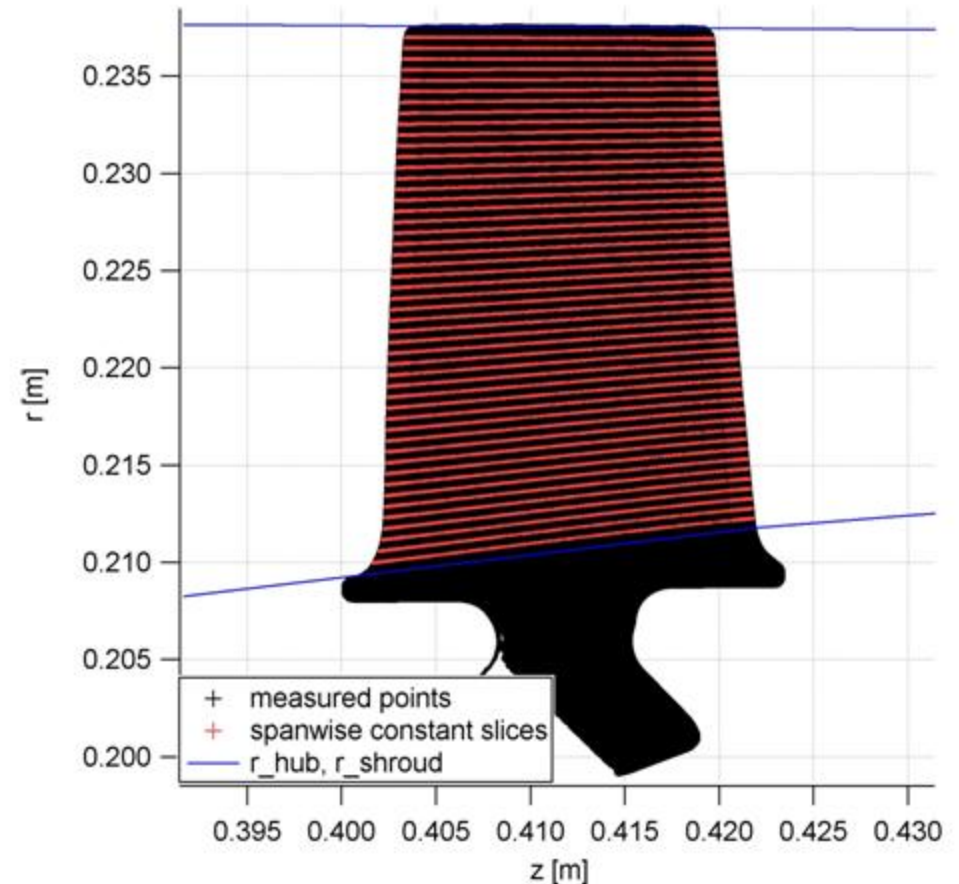


- Introduction
- **Parameter model**
- Statistical Analysis
- Probabilistic Simulation

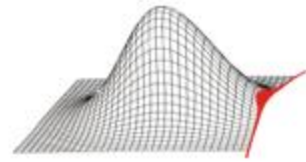


## Way from measured data to parameters

1. sorting of discrete points into slices (spanwise constant)

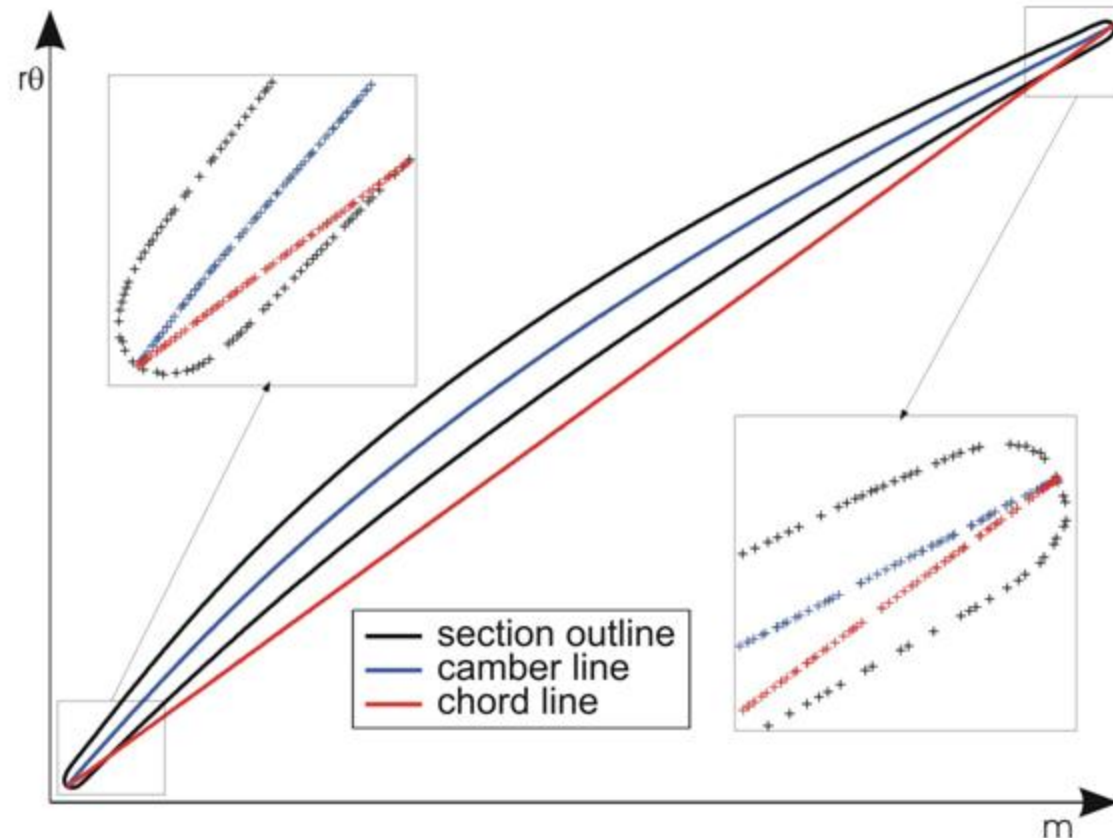


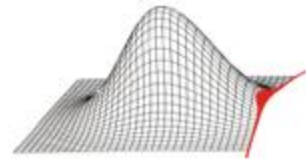




## Way from measured data to parameters

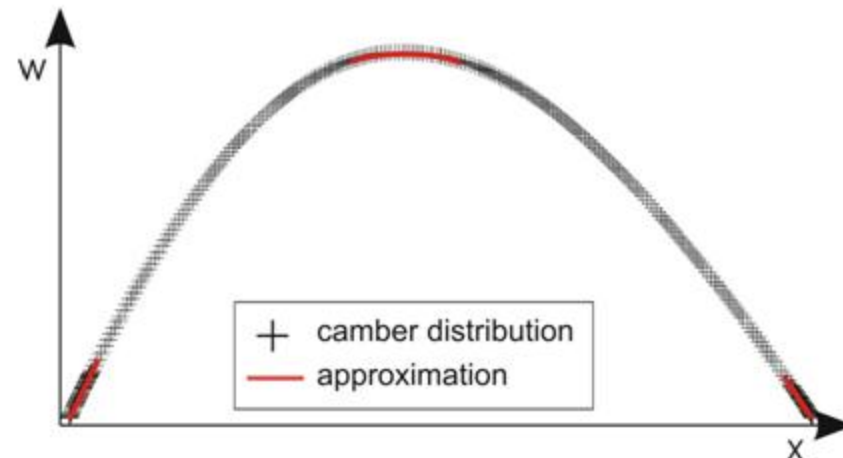
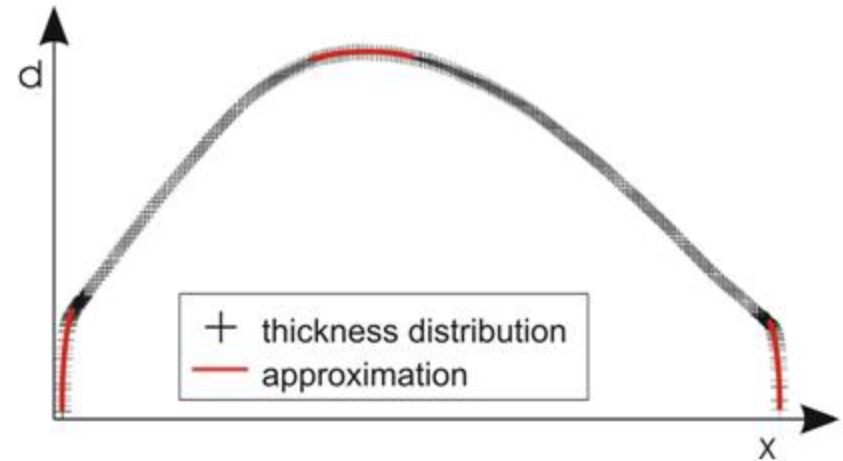
1. sorting of discrete points into slices (spanwise constant)
2. section outline trough rotation symmetric face
3. calculation of camber line and chord line

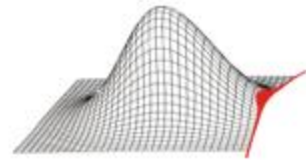




## Way from measured data to parameters

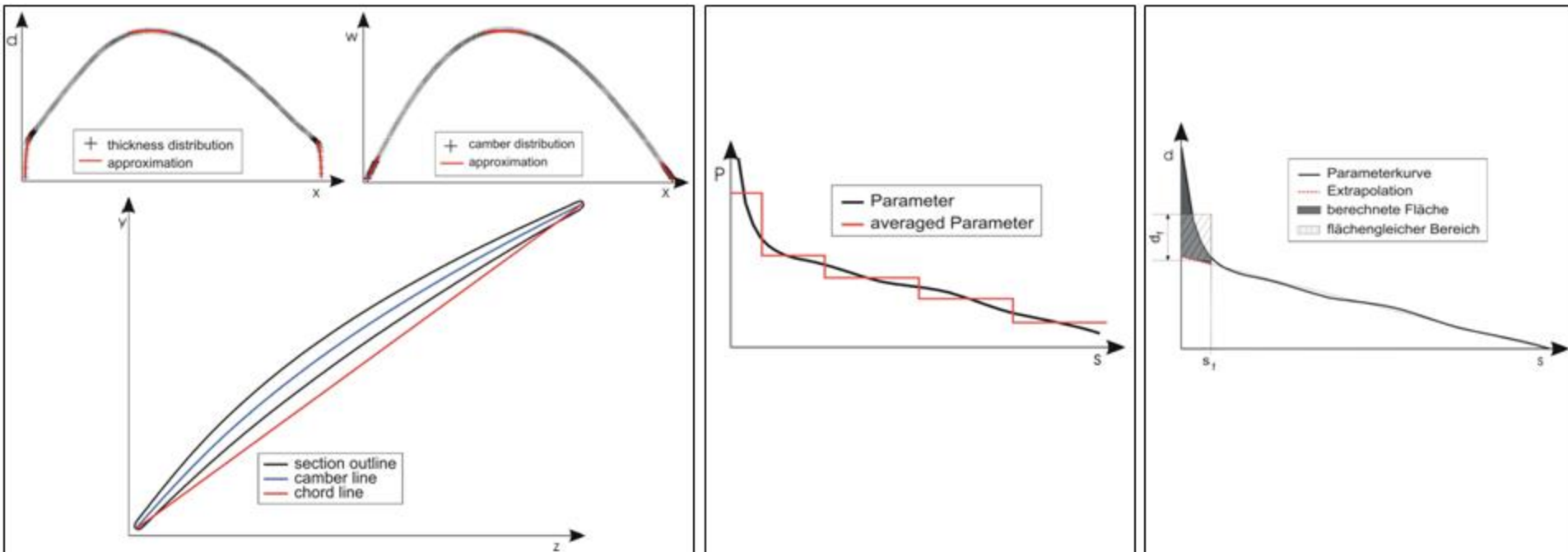
1. sorting of discrete points into slices (spanwise constant)
2. section outline trough rotation symmetric face
3. calculation of camber line and chord line
4. calculation of camber and thickness distribution

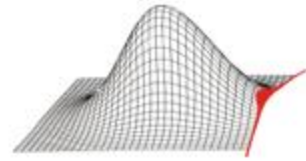




## Parameter model – number of parameters for blade

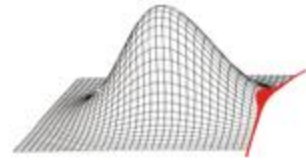
parameters/section (14) \* no of sections + parameters for fillet (2)



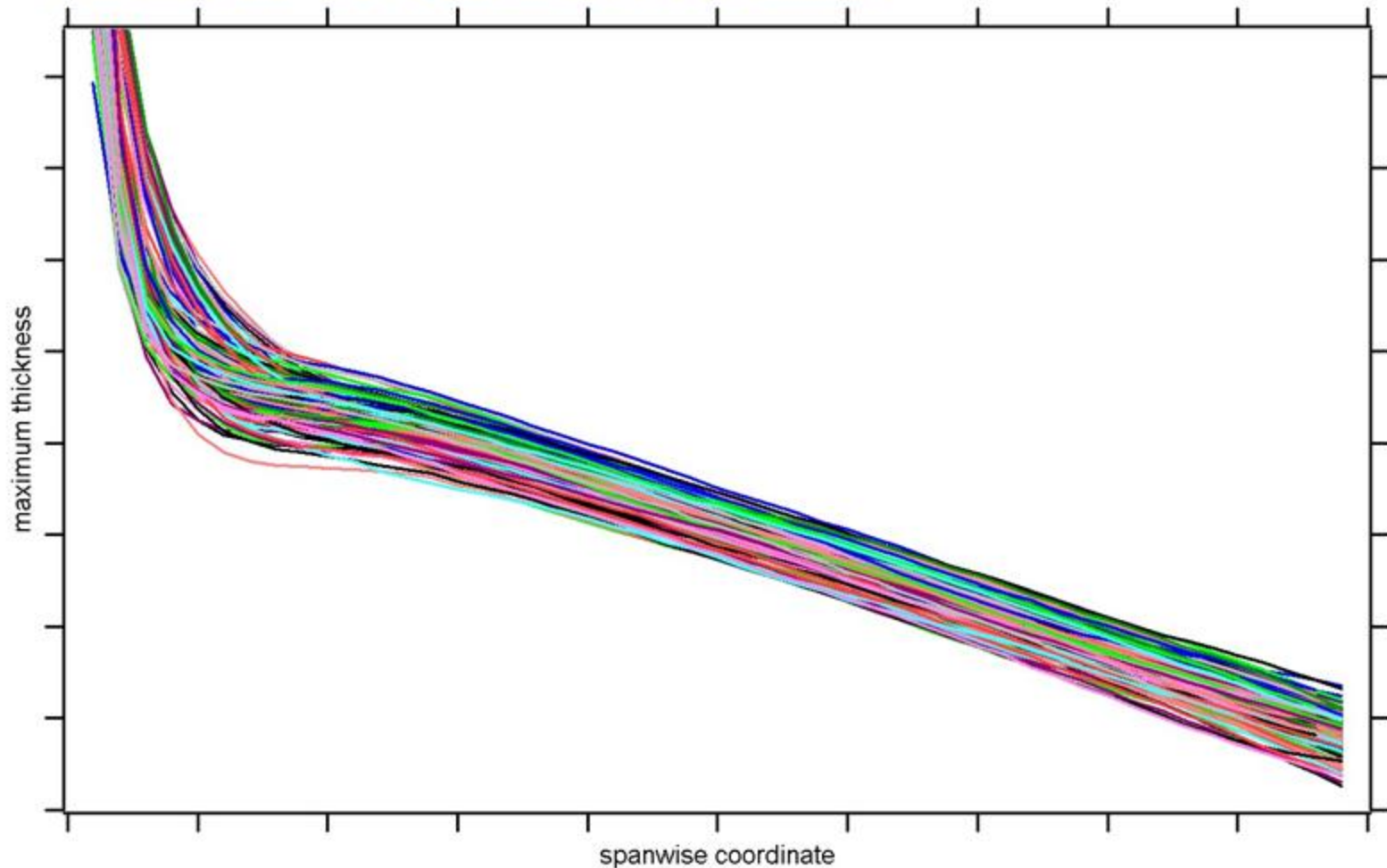


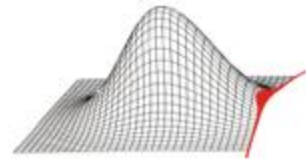
- Introduction
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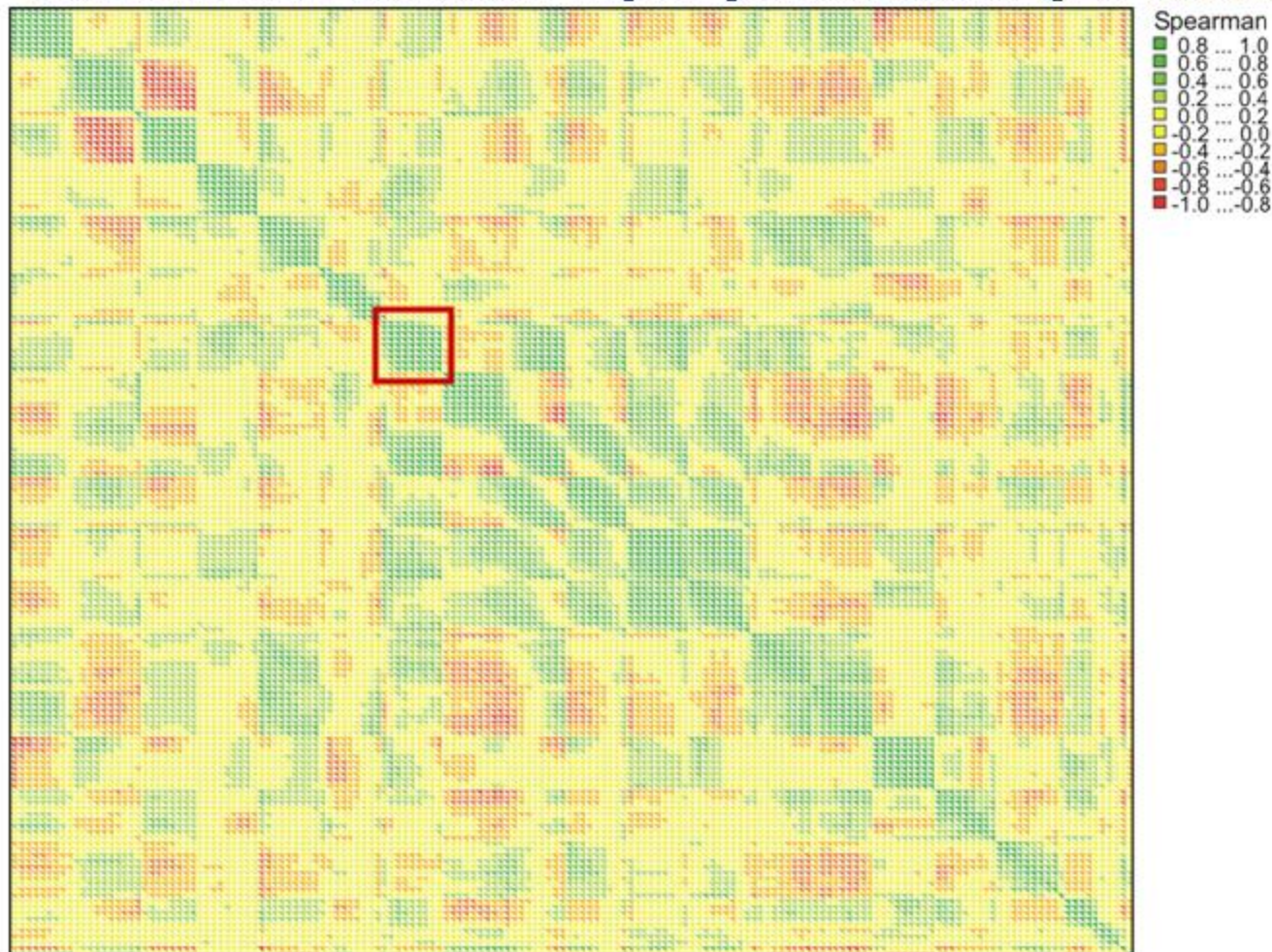


## Parameter vs. spanwise coordinate

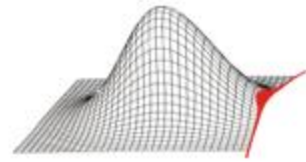




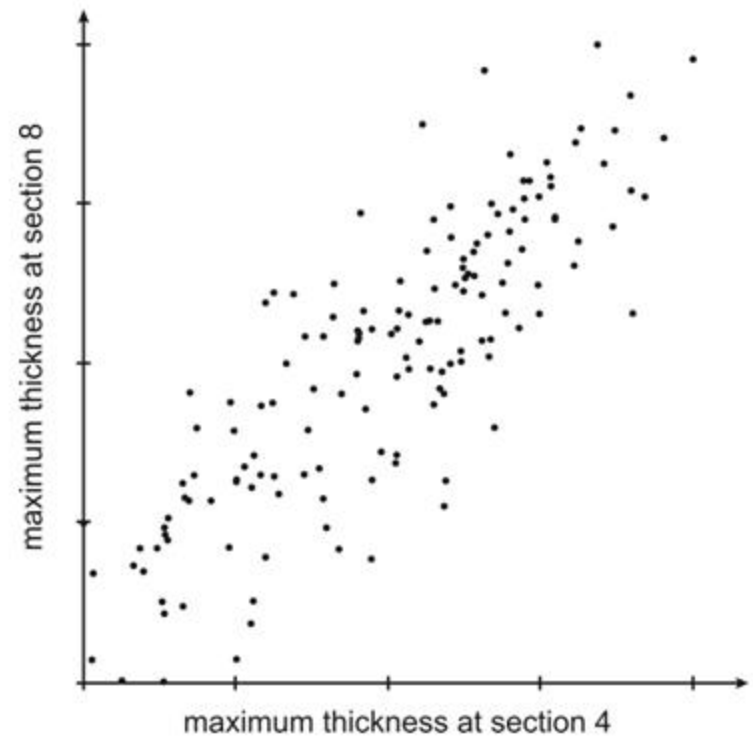
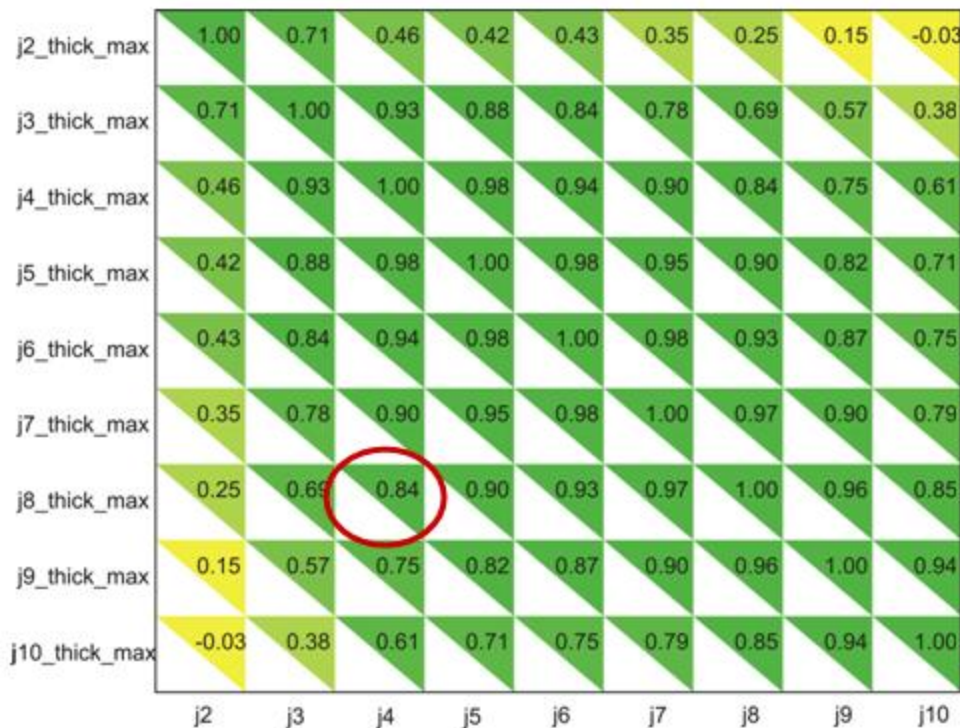
## Correlation between input parameters (10 sections)

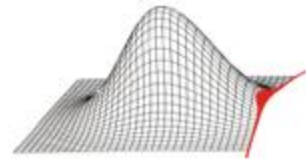






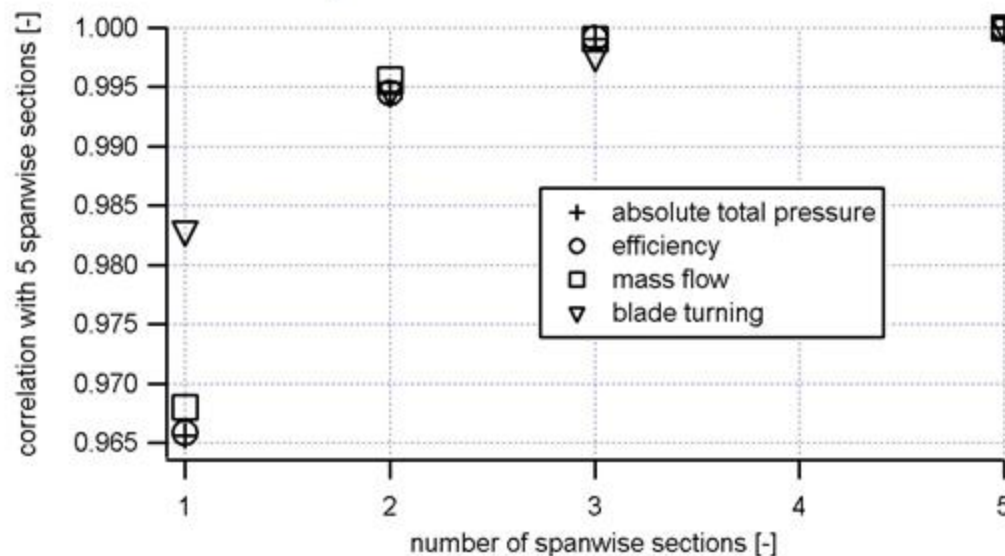
## Correlation between input parameters (10 sections)



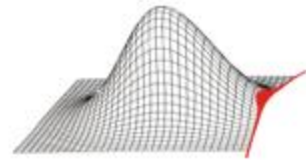


## How many averaged sections are needed?

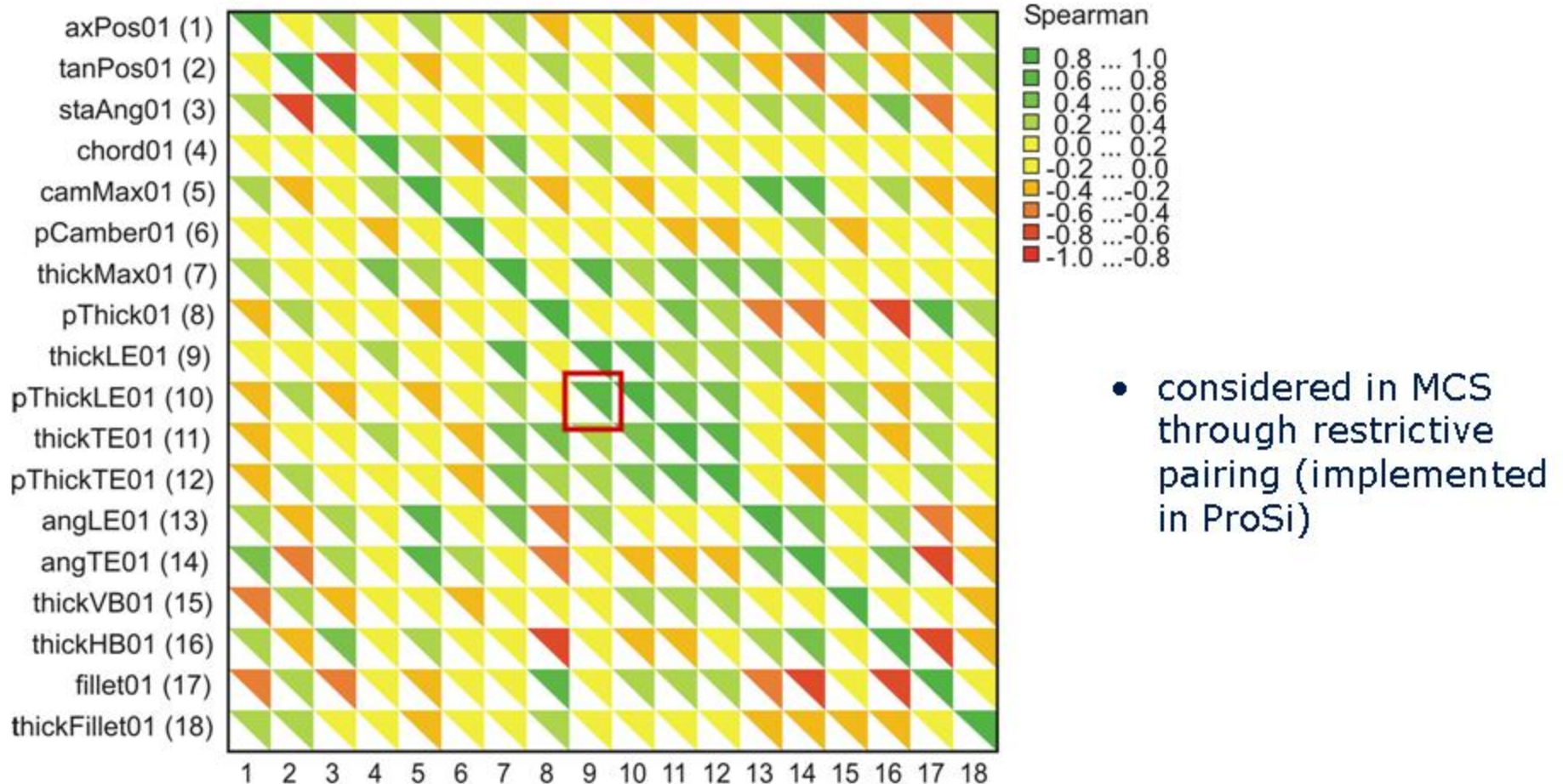
- calculation of scanned blades (no probabilistic methods used)
- determine required number of spanwise averaged sections (1 vs. 2 vs. 3 vs. 5)



- 1 spanwise averaged section captures dominating effects
- advantages in post processing

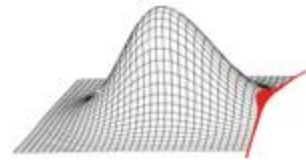


## Correlation between input parameters (1 section)

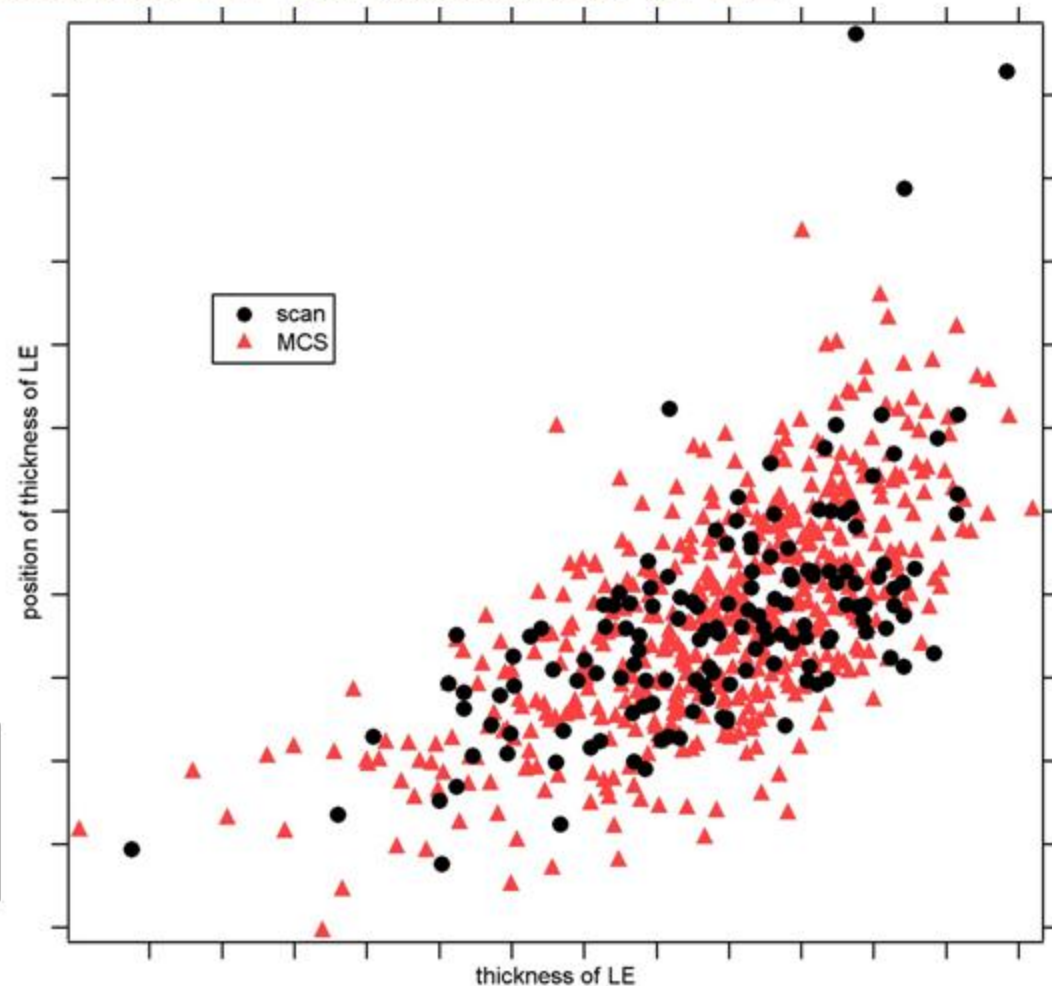
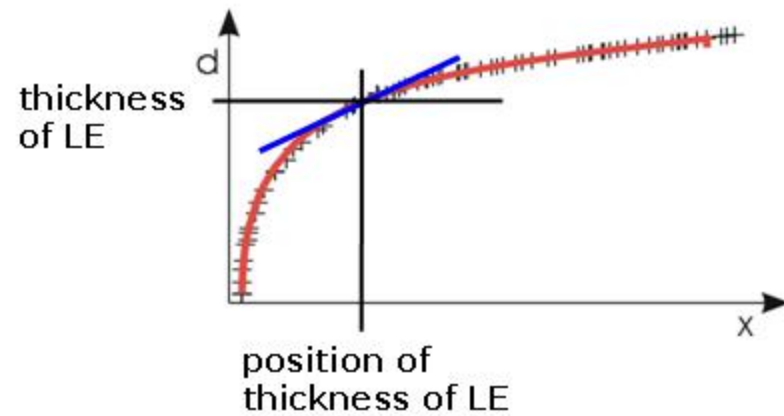


- considered in MCS through restrictive pairing (implemented in ProSi)

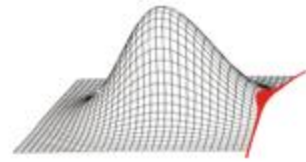




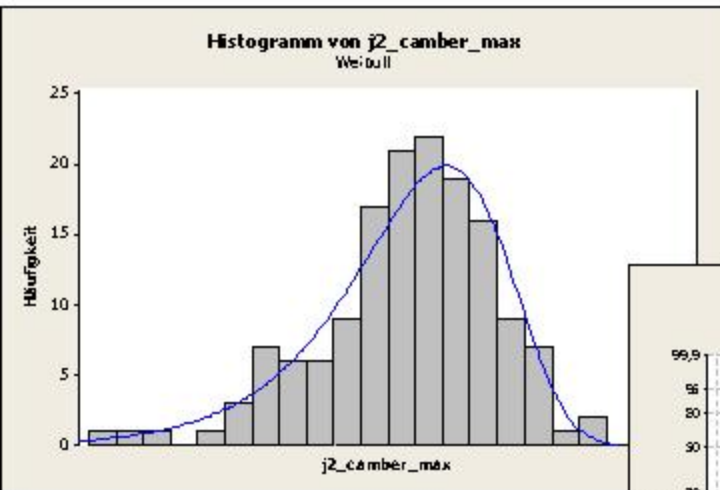
## Ant-Hill-Plot: pos of thickness LE vs. thickness of LE



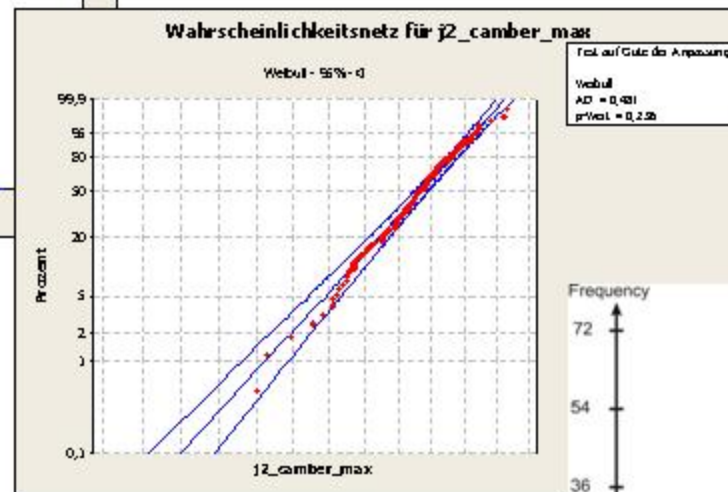
→ correlation of thickness of LE  
 with position of thickness of LE  
 → tendency to circular shape



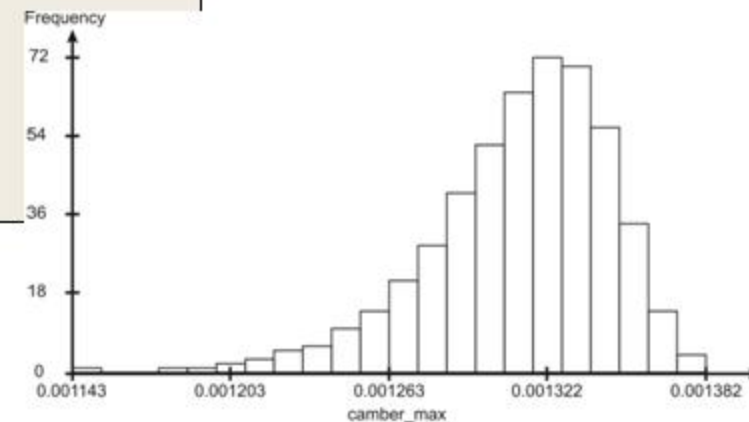
## Fitting of determined distributions

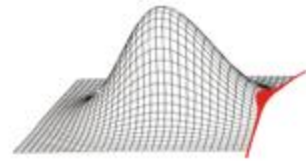


- Minitab
- best distribution through min. AD-value

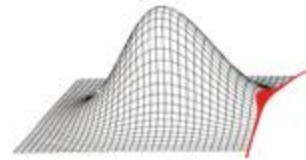


- ProSi
- MCS with 500 shots using LHS



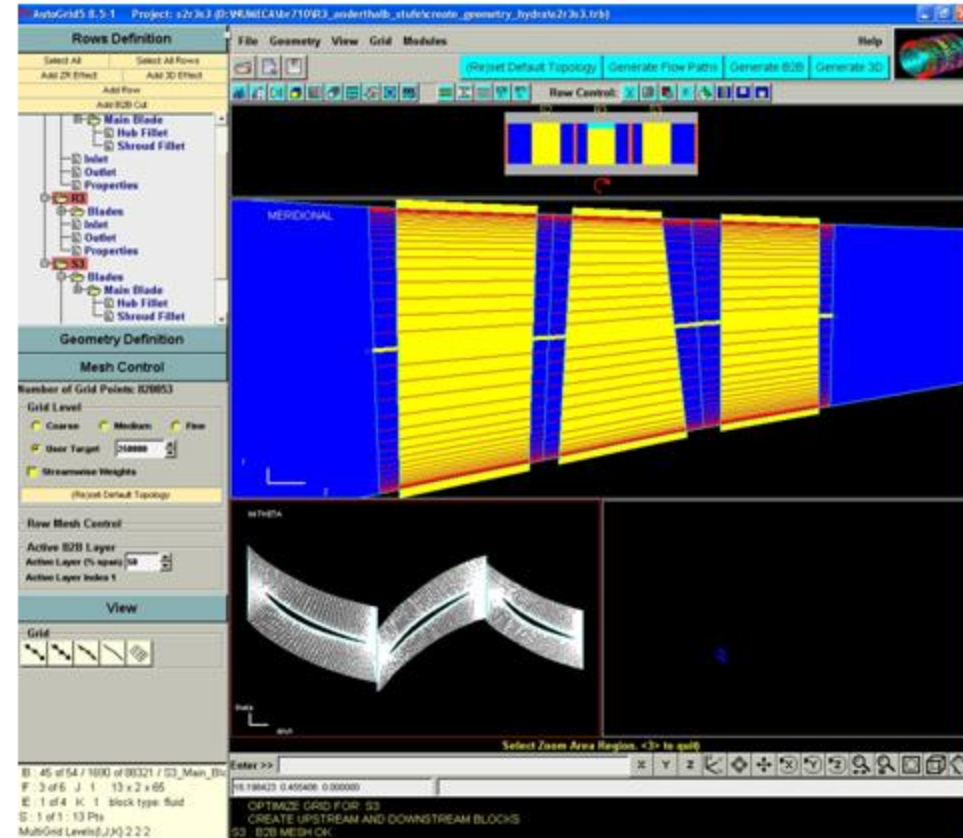


- Introduction
- Parameter model
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- **Probabilistic Simulation**

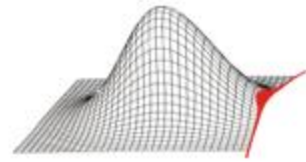


## Model

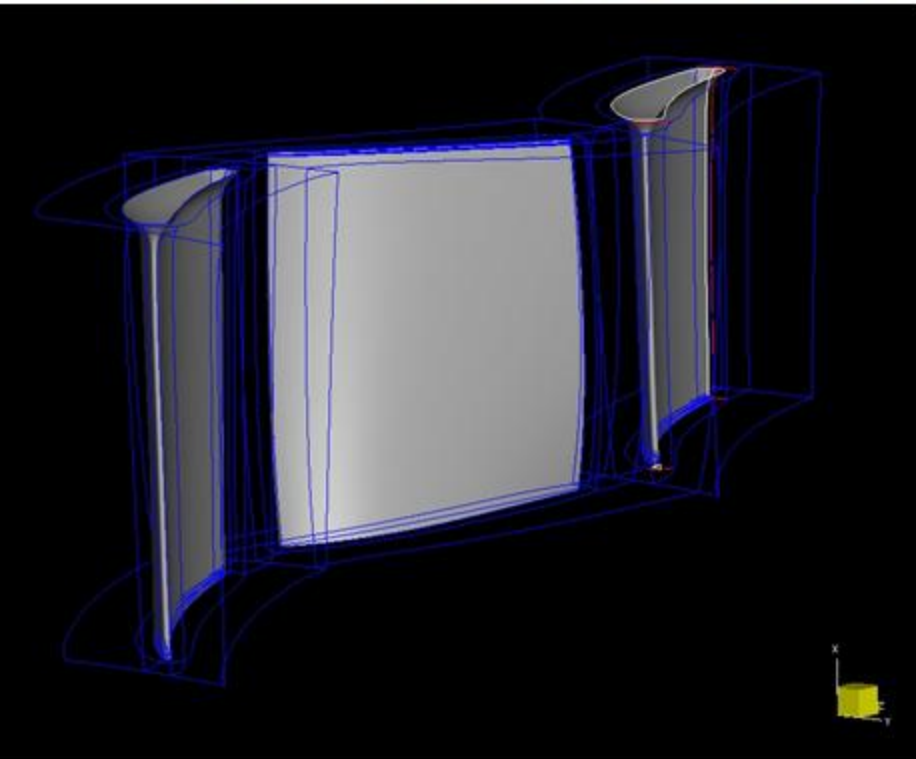
- CFD-Model:
  - 1.5 HPC-stage of BR710
  - ~300k points per blade
  - $p_t(r)$ ,  $T_t(r)$  and flow angle at inlet and  $p_s(r)$  at outlet defined
- Probabilistic Model:
  - Monte Carlo Simulation with 500 shots
  - consideration correlations between parameters
  - 1 spanwise averaged section used  $\rightarrow$  16 Parameter



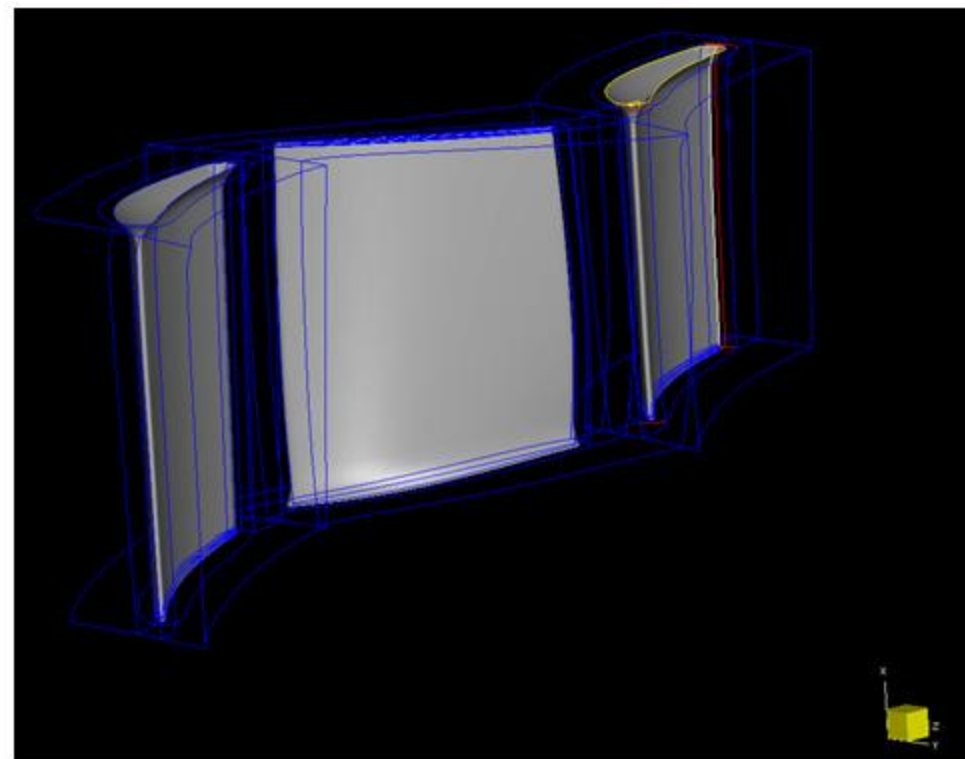




## blade surface of 1.5 stage

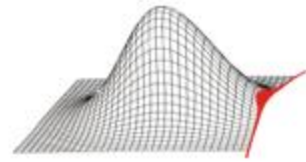


base-mesh



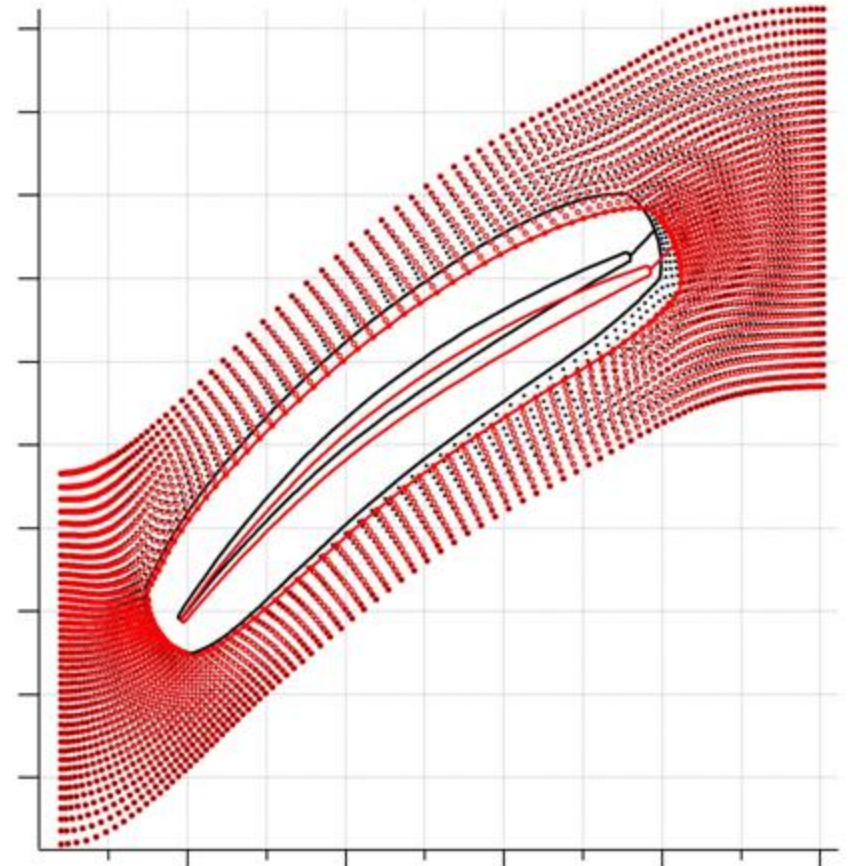
realization



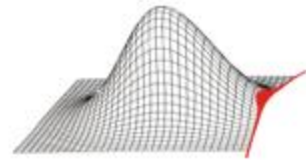


## Mesh-Morphing

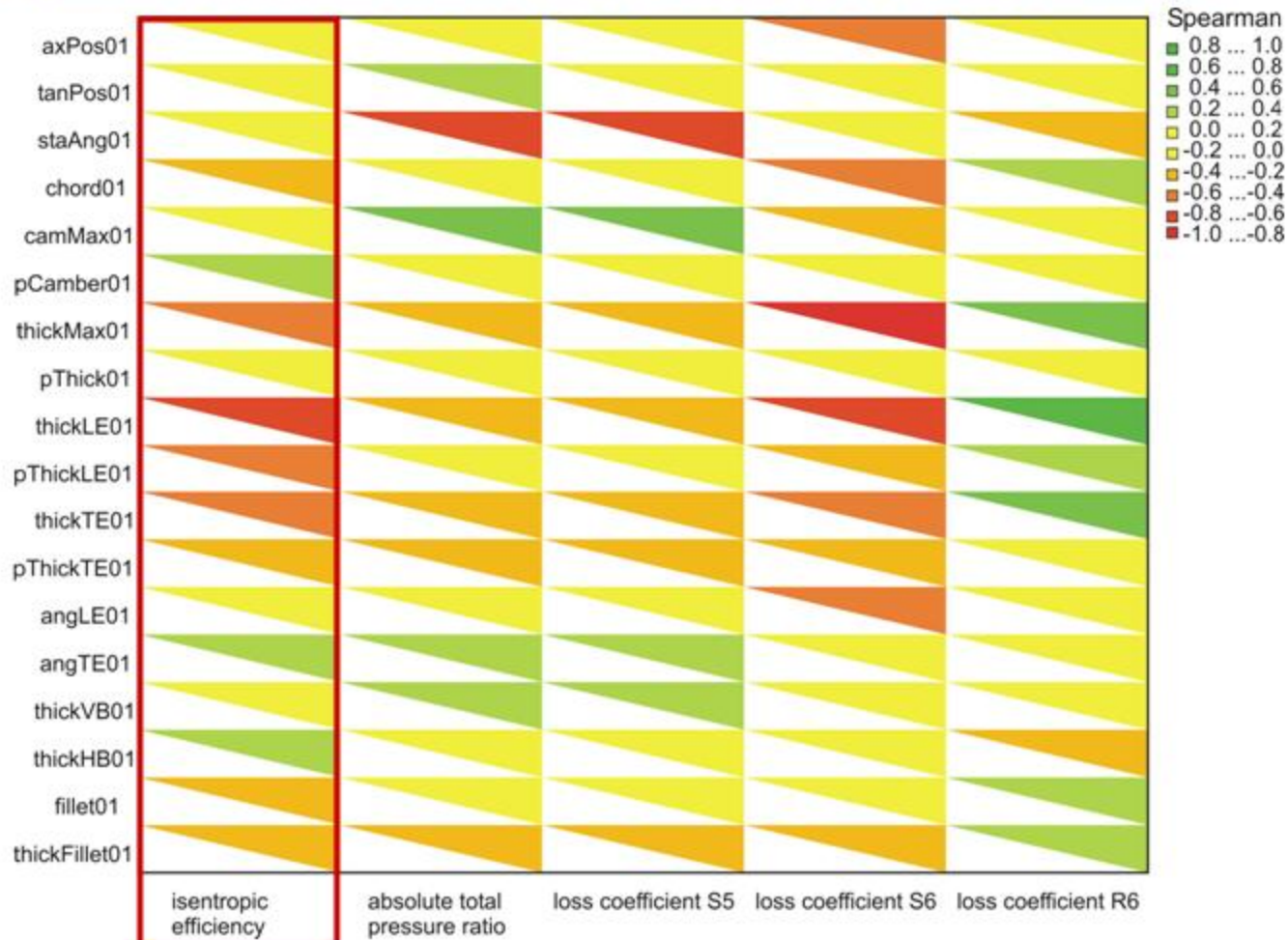
- share the deformation between O-grid and H-grids

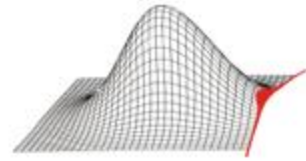






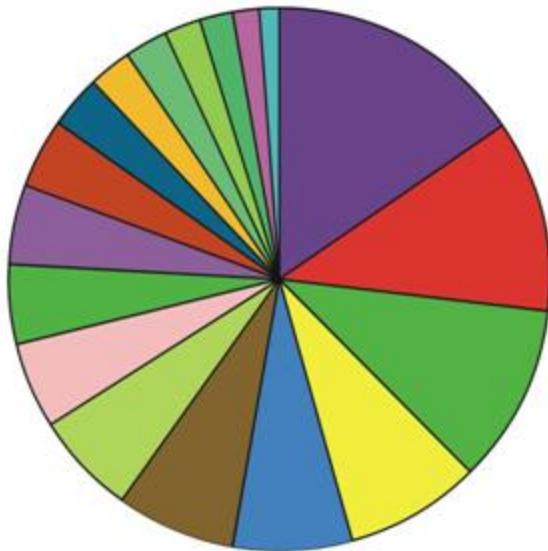
## Correlation coefficients: input vs. output variables



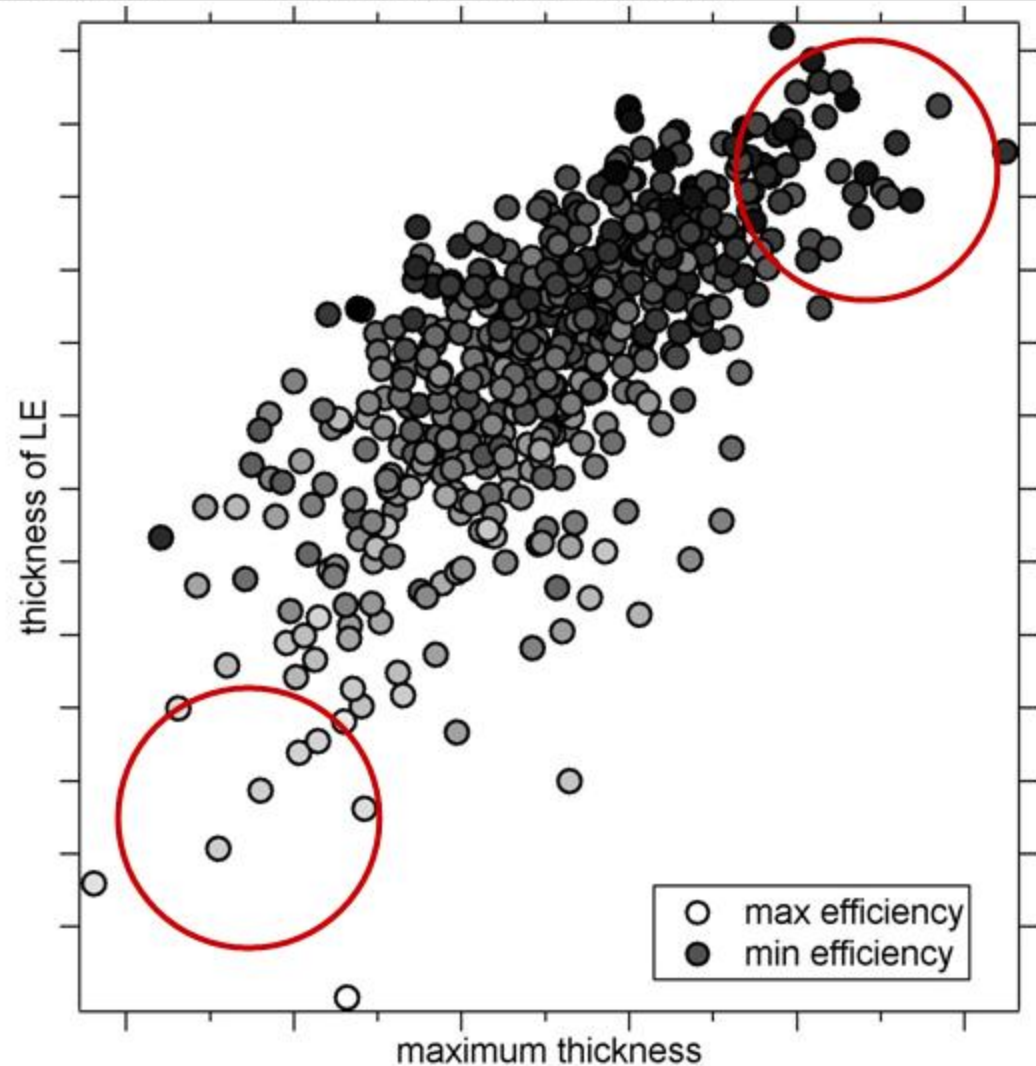


## pie chart

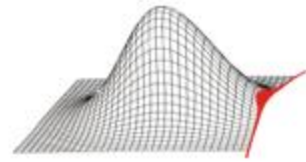
Target-Variable: Isentropic efficiency



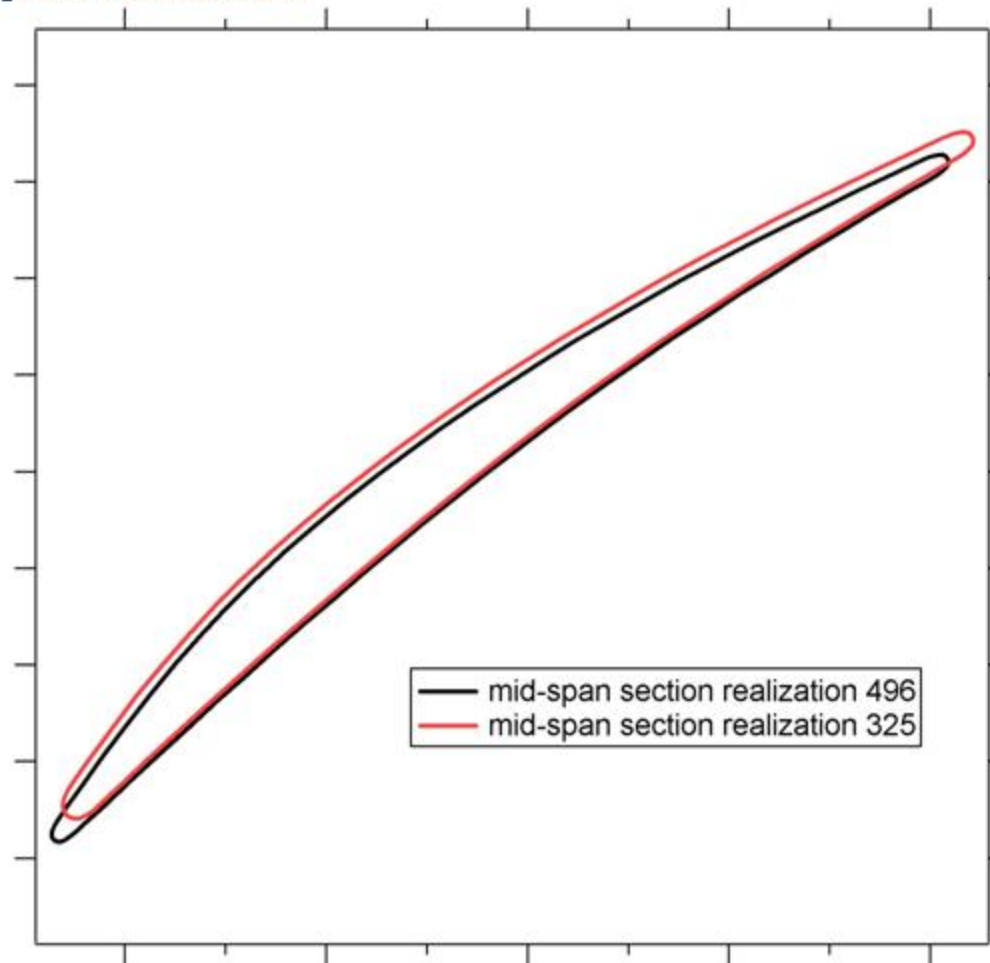
- thickLE01
- thickMax01
- thickTE01
- pThickLE01
- pThickTE01
- thickFillet01
- chord01
- angTE01
- thickHB01
- fillet01
- pCamber01
- staAng01
- angLE01
- tanPos01
- thickVB01
- pThick01
- camMax01
- axPos01







## mid-span section

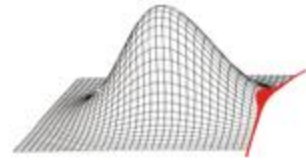


### analysis of 2 blades:

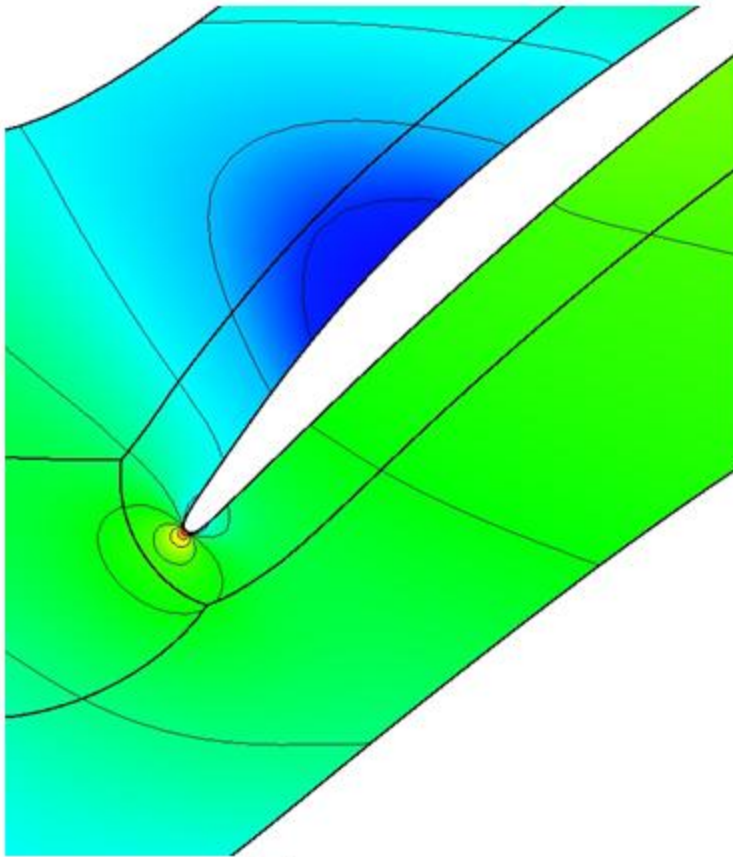
realization 325

- thick blade
  - low efficiency
- realization 496
- thin blade
  - high efficiency

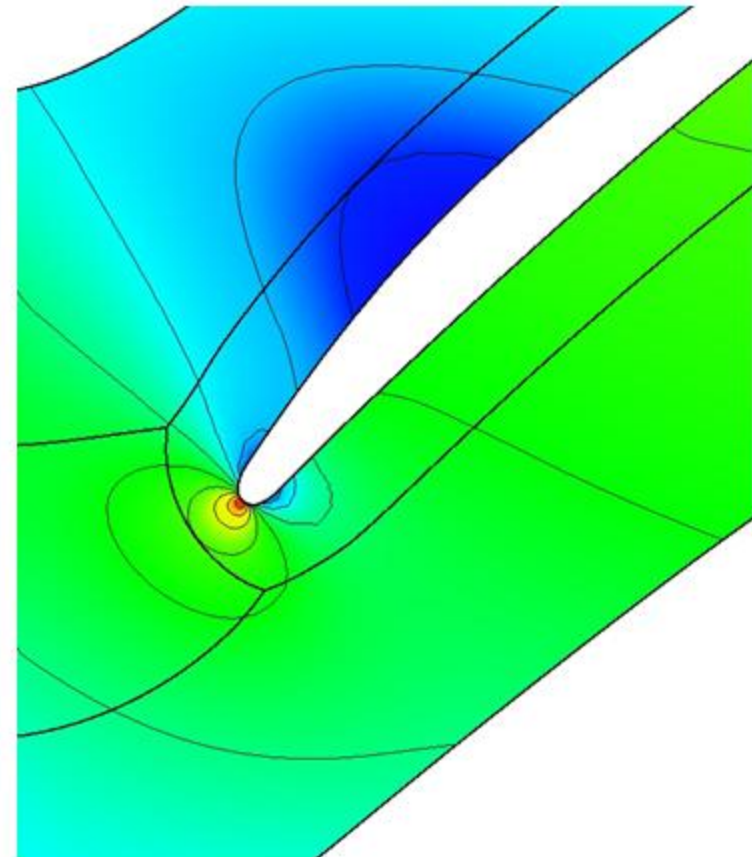




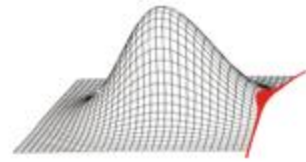
## static pressure at mid-span



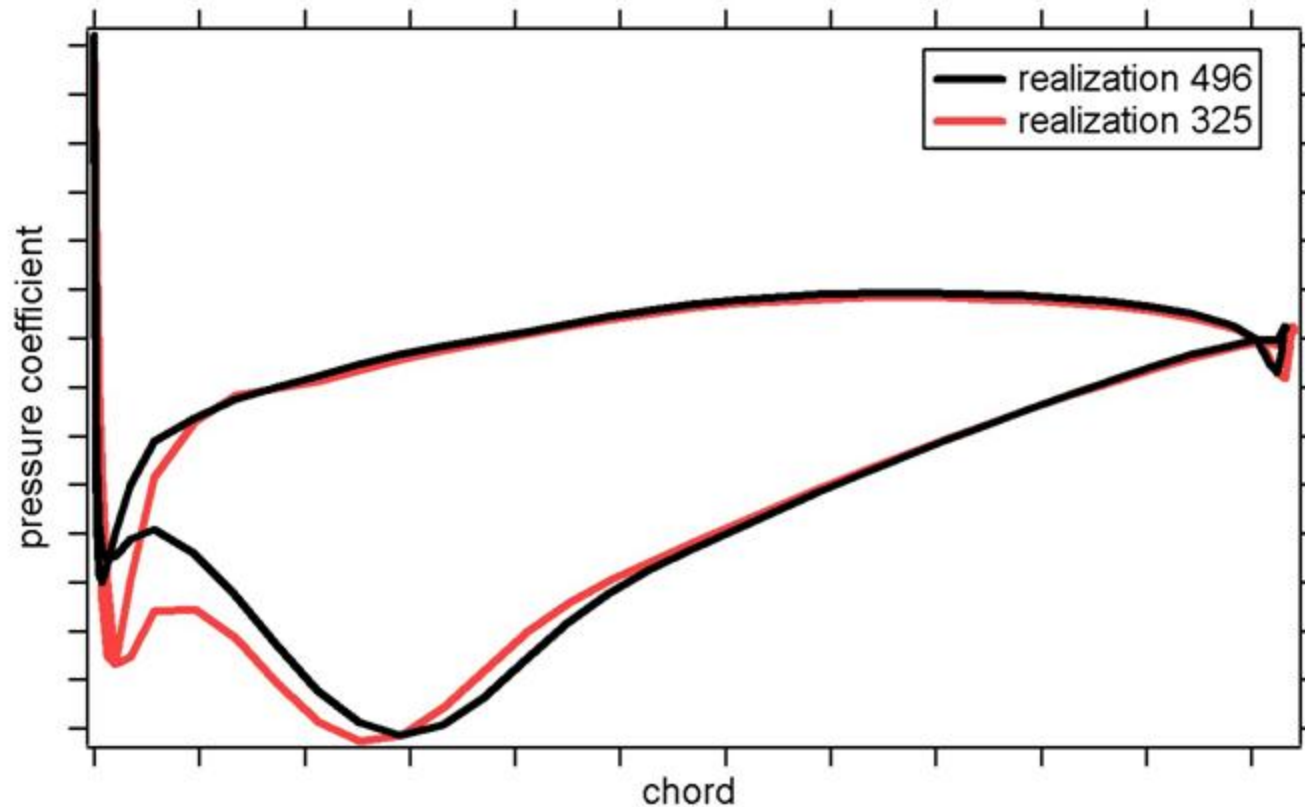
rel 496



rel 325



## static pressure on blade surface (mid-span)



analysis of 2 blades:

realization 325

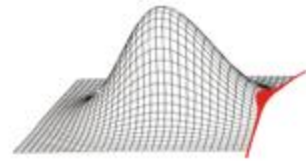
- thick blade

- low efficiency

realization 496

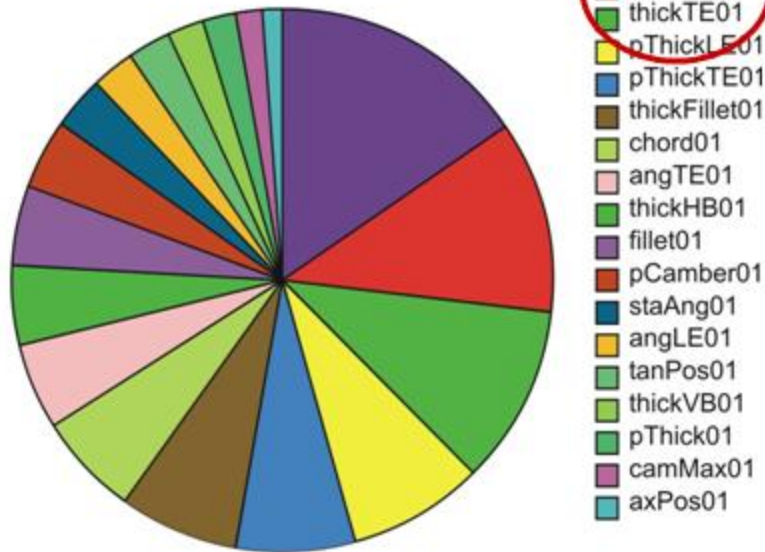
- thin blade

- high efficiency

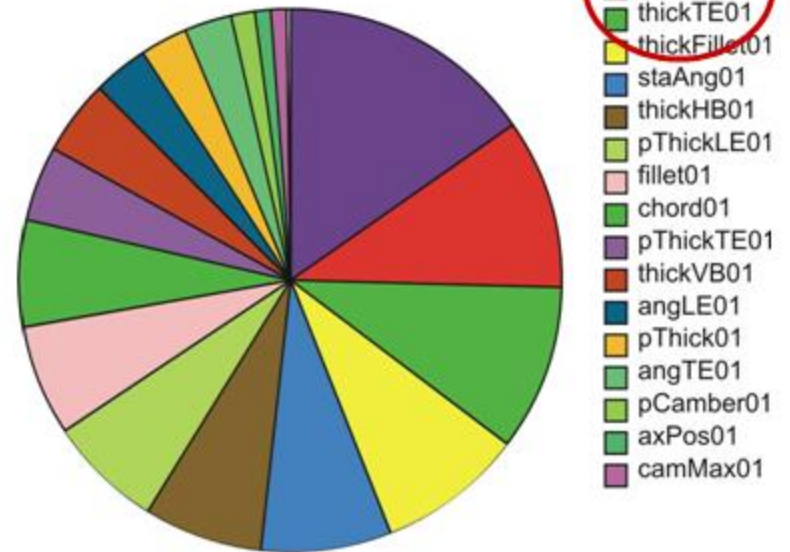


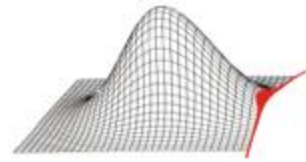
## pie chart analysis: isentropic efficiency and loss coefficient

Target-Variable: Isentropic efficiency

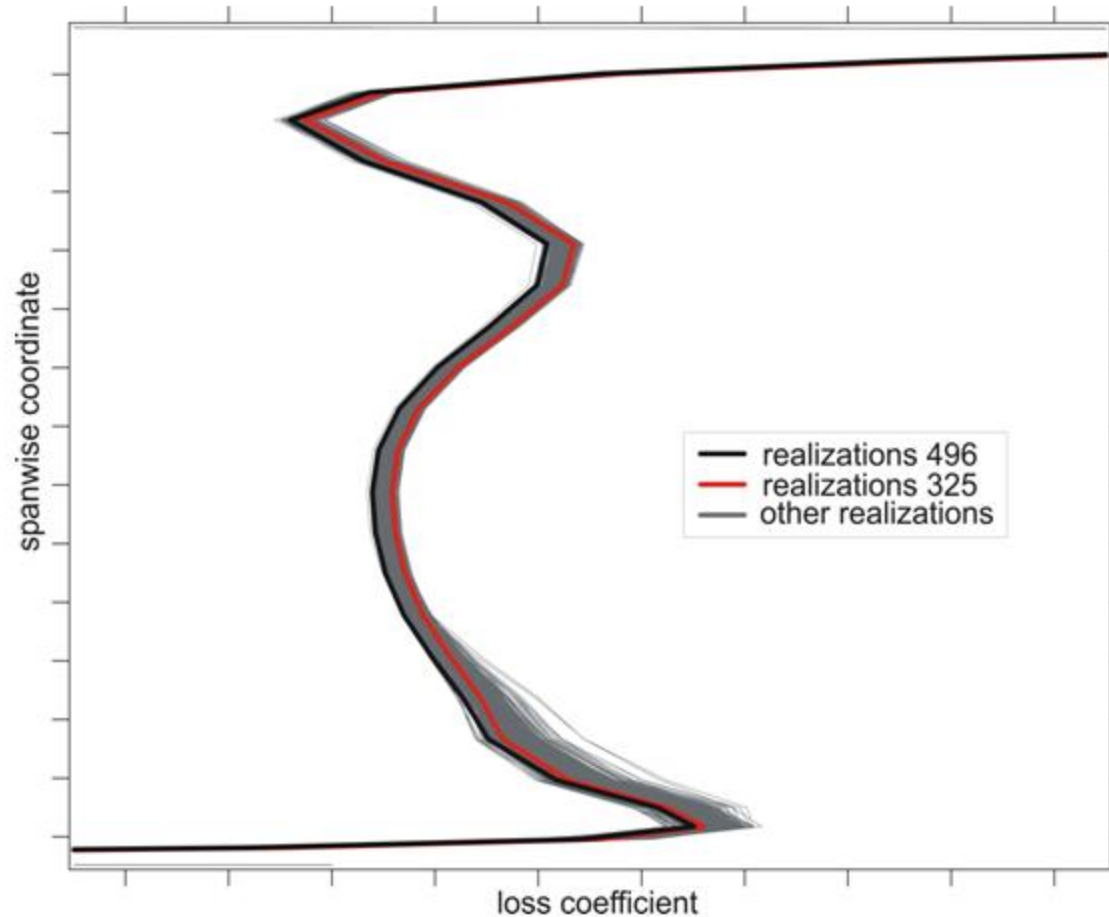


Target-Variable: loss coefficient R6





## loss coefficient

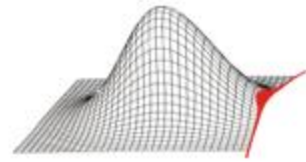


### analysis of 2 blades:

realization 325

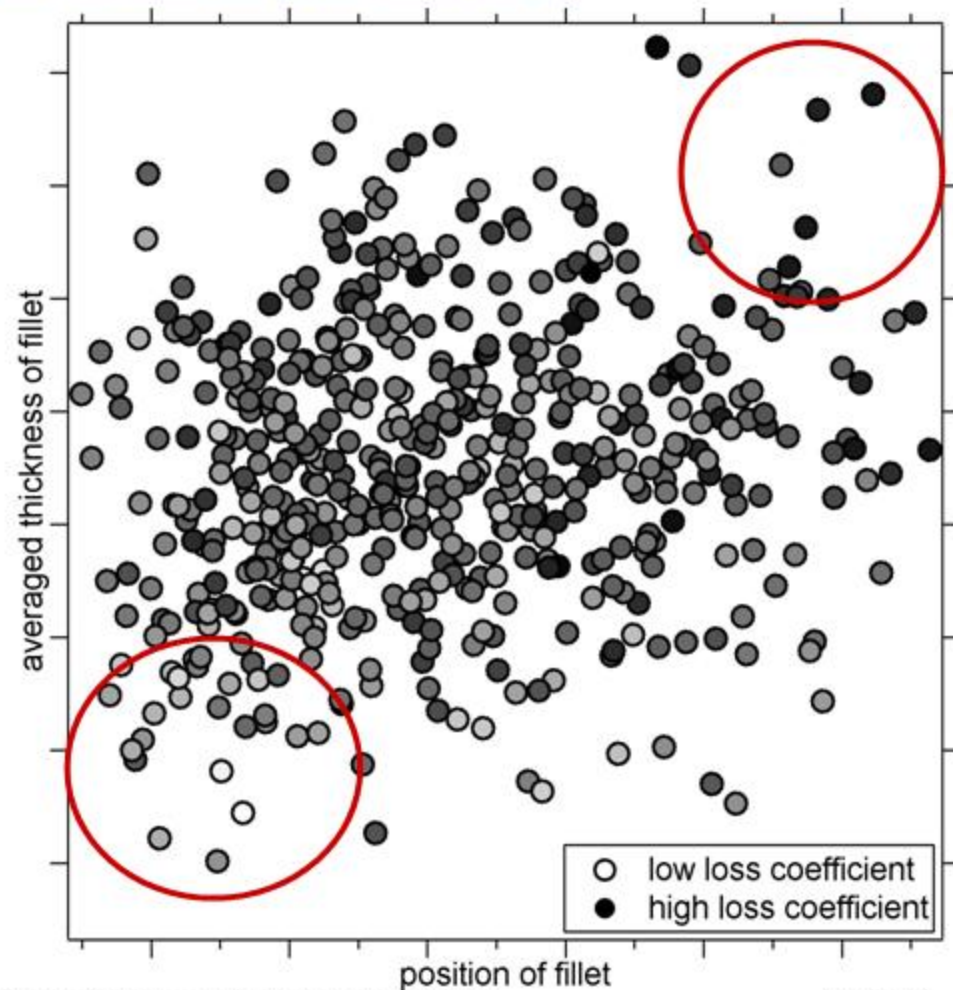
- thick blade
  - low efficiency
- realization 496
- thin blade
  - high efficiency



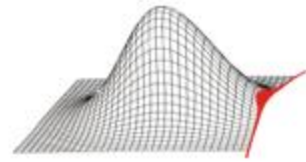


## sensitivity of loss coefficient to fillet parameters

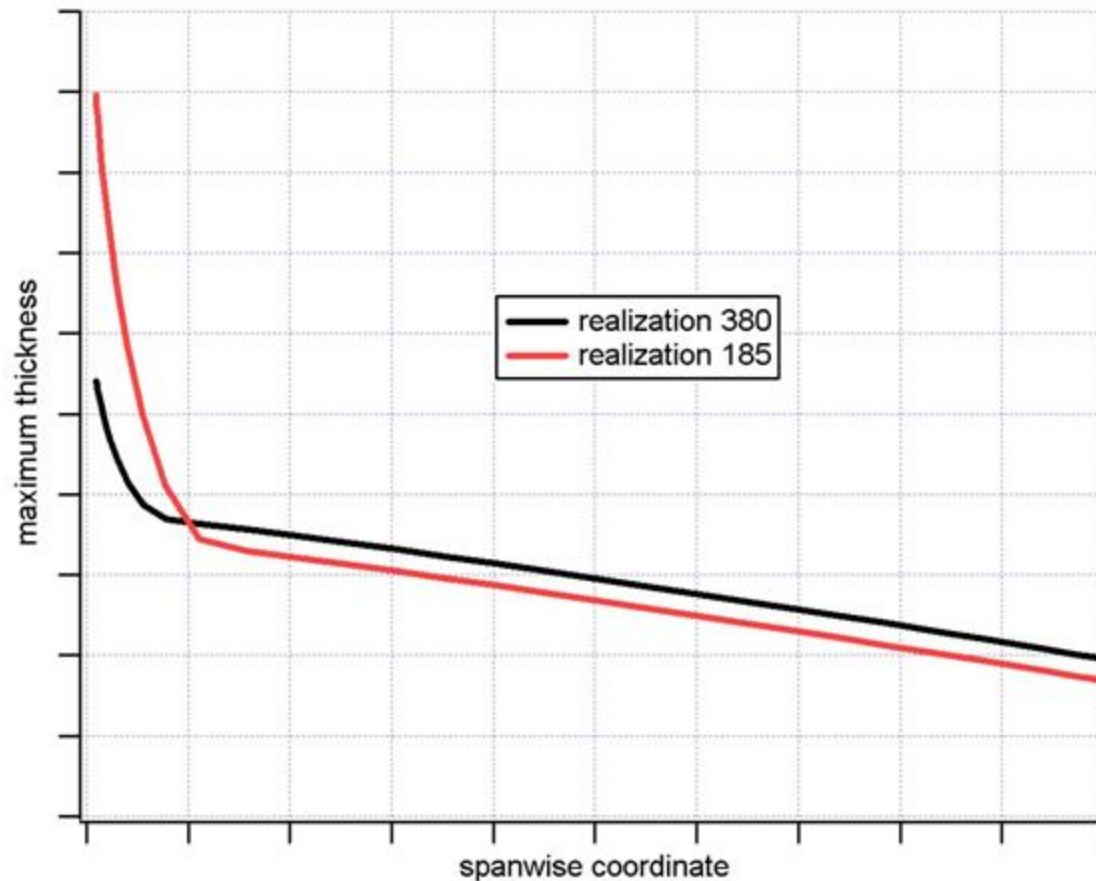
analysis of 2 blades:  
realization 380  
•small fillet  
•lower loss coefficient  
realization 185  
•big fillet  
•higher loss coefficient



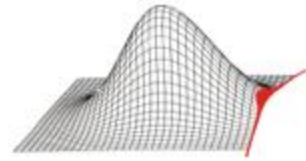




## thickness distribution: two selected realizations

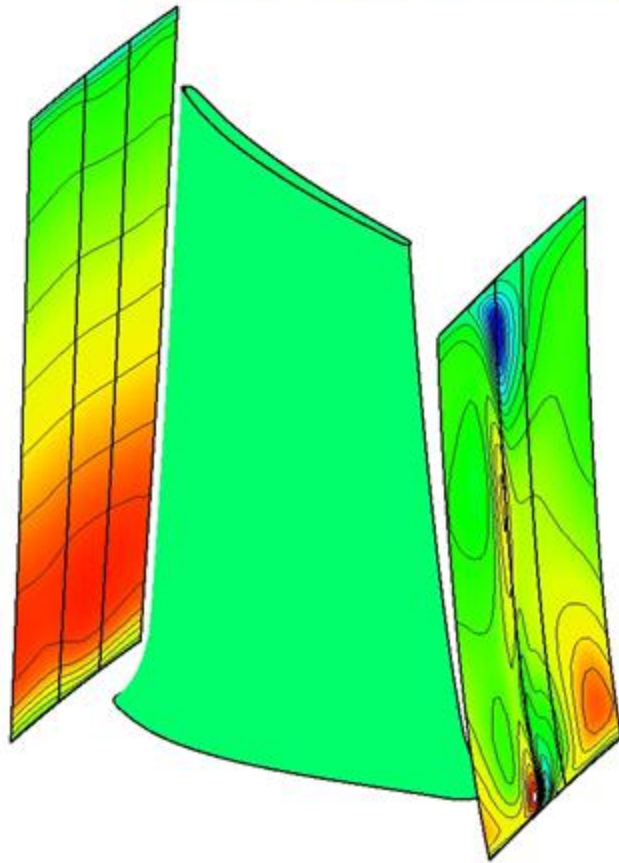


analysis of 2 blades:  
 realization 380  
 •small fillet  
 •lower loss coefficient  
 realization 185  
 •big fillet  
 •higher loss coefficient



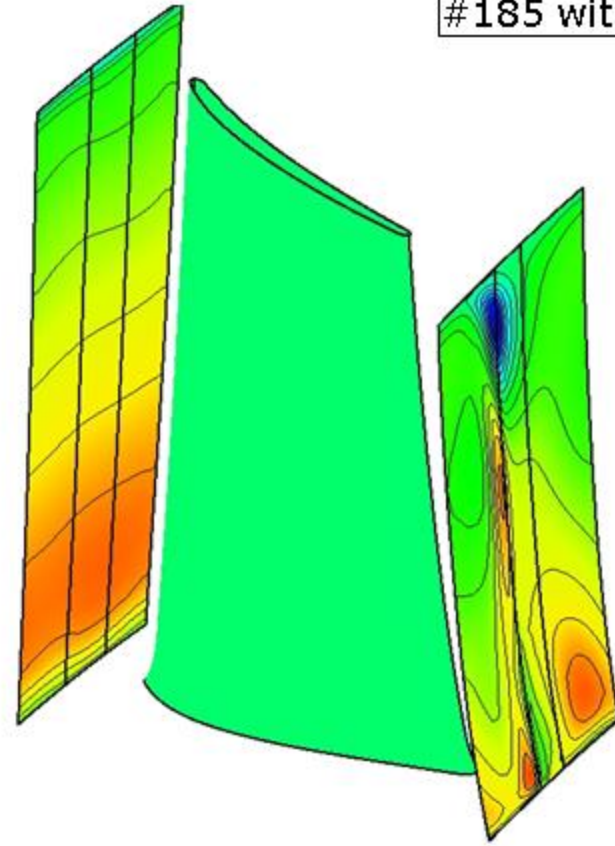
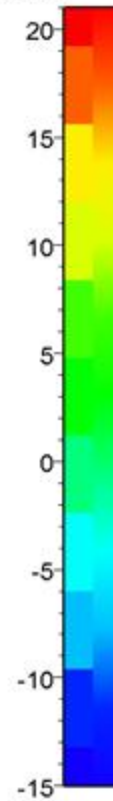
## radial velocity: two selected realizations

analysis of 2 blades:  
#380 with small fillet  
#185 with big fillet



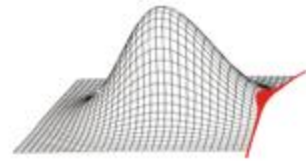
rel 185

$V_r$  (m/s)

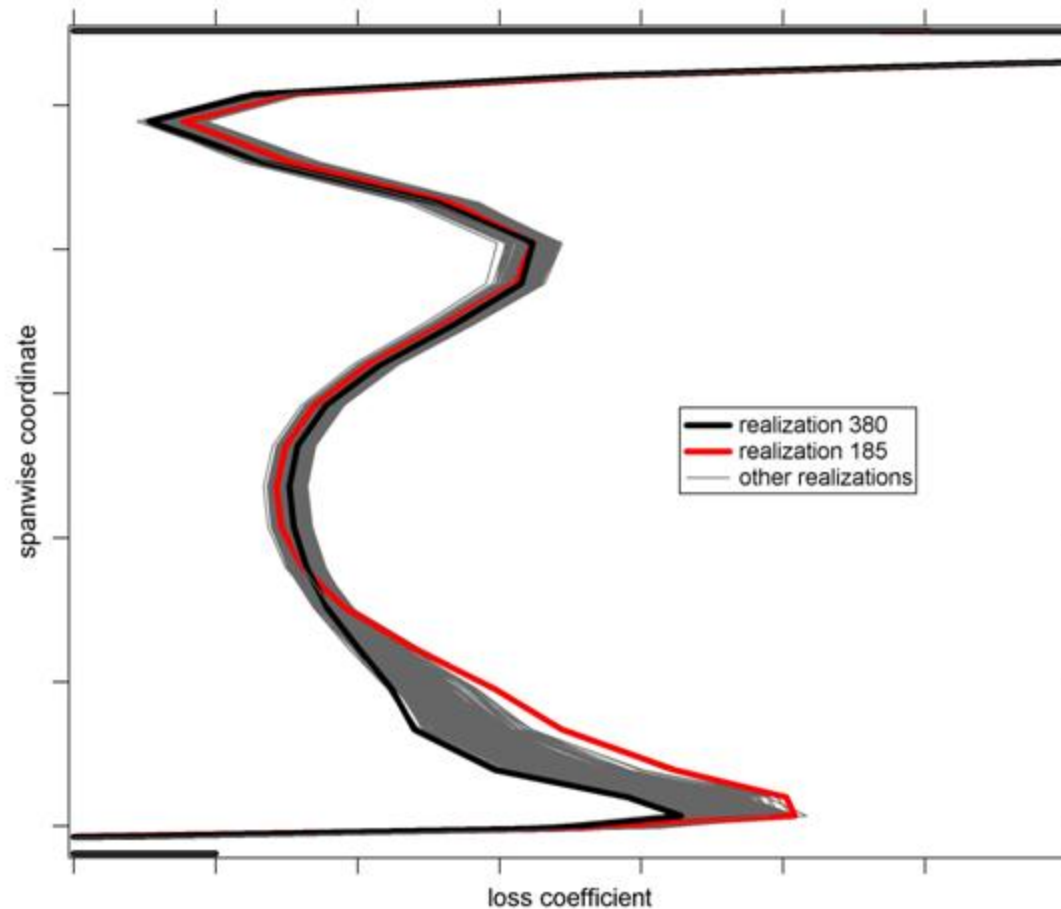


rel 380

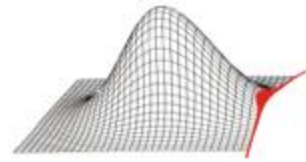




## sensitivity of loss coefficient to fillet parameters

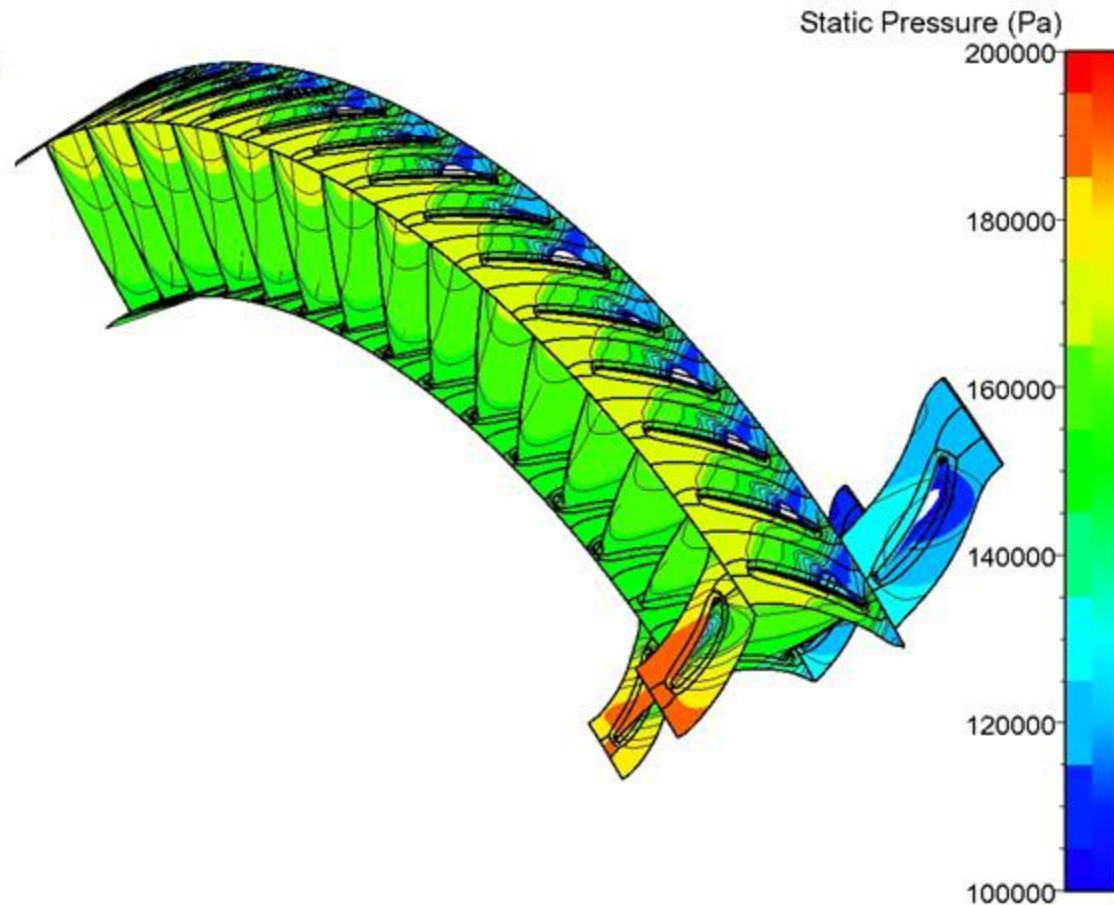


analysis of 2 blades:  
 realization 380  
 •small fillet  
 •lower loss coefficient  
 realization 185  
 •big fillet  
 •higher loss coefficient

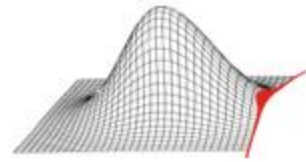


## further probabilistic Simulation

- HPC-stage analysis with up to 15 individual blades
- $15 \cdot 16 = 240$  probabilistic variables used
- investigation of non-axial symmetric effects
- developed morphing approach allows quick grid generation







# Thank you for your Attention!